UNIT 2 Integers and Algebra

Chapter 3

Algebra: Integers

Chapter 4

Algebra: Linear Equations and Functions

Your study of math includes more than just whole numbers and decimals. In this unit, you will use negative numbers to describe many real-life situations and you will solve and graph equations that represent them.

102 Unit 2 Integers and Algebra Mike Powell/Getty Images



INTERDISCIPLINARY PROJECT

The Wide World of Soccer

Math and Geography Soccer fans, get up on your feet! You've been selected by an elite committee to join us on a world-wide soccer adventure. Along the way, you'll be gathering data about the geography of countries where soccer is the favorite sport. You'll also make some predictions about the future of soccer in the United States. We will be leaving on our adventure very shortly, so pack your math tools and your thinking cap. This is one adventure you don't want to miss.

CONTENTS



by Log on to msmath2.net/webquest to begin your WebQuest.





What does lightning have to do with math?

Have you heard of the phrase "opposites attract"? During thunderstorms, negatively-charged electrons in the clouds are attracted to positively-charged protons on the ground. This opposite attraction causes lightning. In mathematics, you can use opposites to help you add and subtract positive and negative integers.

CONTENTS

You will solve problems about thunderstorms in Lesson 3-4.

GETTING STARTED

CONTENTS

Diagnose Readiness

Take this quiz to see if you are ready to begin Chapter 3. Refer to the lesson or page number in parentheses for review.

Vocabulary Review

State whether each sentence is *true* or *false*. If *false*, replace the underlined word to make a true sentence.

- 1. The <u>mean</u> of 1, 3, and 6 is 3. (Lesson 2-4)
- 2. The difference between the greatest number and the least number in a set of data is called the range. (Lesson 2-3)

Prerequisite Skills

Replace each ● with < or > to make a true sentence. (Page 556)

3 . 1,458 ● 1,548	4 . 36 • 34
5 . 1.02 ● 1.20	6 . 76.7 • 77.6
Add.	
7. 84 + 39	8. 198 + 289
9. 826 + 904	10 . 3,068 + 5,294

Multiply.

11.	$2 \cdot 5 \cdot 3$	12.	$18 \cdot 9$
13.	$15 \cdot 6$	14.	$10 \cdot 4 \cdot 7$

Divide.

15.	63 ÷ 9	16.	96 ÷ 12
17.	125 ÷ 5	18.	187 ÷ 17

Find the mean and range for each set of

data. (Lessons 2-3 and 2-4)

19 . 12 <i>,</i> 8 <i>,</i> 25 <i>,</i> 16 <i>,</i> 9	20 . 34, 57, 60, 45
--	----------------------------

FOLDABLES Study Organiture 81/2	tegers Make this Foldable help you organize formation about integers. gin with two sheets of $-^{''} \times 11''$ paper.
Fold and Cut On Fold in half from bottom. Cut alo from edges to n	e Sheet n top to ng fold nargin.
Fold and Cut the Other Sheet Fold in half from bottom. Cut alo between margin	n top to ng fold ns.
Fold Insert first sheet through second and align folds.	sheet
Label Label Each page	with a Anticept of Absolute Value
Noteables!	Chapter Notes Each
throughout the cha Interactive Study No or your own notebo your chapter notes	time you find this logo pter, use your <i>Noteables™:</i> <i>otebook with Foldables™</i> ook to take notes. Begin with this Foldable activity.
COLUMN DESCRIPTION OF THE	TANK A TANK DESIGNATION OF THE OWNER
Readin chapter msmat	ess To prepare yourself for this with another quiz, visit h2.net/chapter_readiness

What You'll LEARN

Read and write integers, and find the absolute value of an integer.

NEW Vocabulary

integer graph positive integer negative integer absolute value

MATH Symbols

- positive three +3
- -3 negative three
- 3 absolute value of three

Integers and Absolute Value



when am I ever going to use this?

FOOTBALL The graph shows the number of yards the Bears gained or lost on the first four downs. A value of -3 represents a 3-yard loss.

- **1**. What does a value of -2represent?
- **2**. On which down did they lose the most yards?
- 3. How can you represent a gain of 9 yards?



Numbers like 9 and -2 are called integers. An **integer** is any number from the set $\{..., -4, -3, -2, -1, 0, 1, 2, 3, 4, ...\}$. Integers can be graphed on a number line. To graph a point on the number line, draw a point on the line at its location.



EXAMPLES Write Integers for Real-Life Situations

WEATHER Write an integer for each situation.

The average temperature in Tennessee for May was 5 degrees below normal.

Because it represents *below* normal, the integer is -5.

The average rainfall in Virginia for November was 5 inches above normal.

Because it represents *above* normal, the integer is +5 or 5.

Your Turn Write an integer for each situation.

a. 6 degrees above normal **b.** 2 inches below normal



READING Math

Set Theory The number 5 is an *element*, or member, of the set of integers. The set $\{-5, 5\}$ is a *subset* of the set of integers.



The numbers -5 and 5 are the same distance from 0, but on opposite sides of 0. So, -5 and 5 have the same **absolute value**.



Skill and Concept Check

msmath2.net/extra examples

- 1. Writing Math Describe a situation in everyday life where negative numbers are used.
- **2. OPEN ENDED** On a number line, graph two different points that have the same absolute value.
- 3. Which One Doesn't Belong? Identify the expression that does not have the same value as the other three. Explain your reasoning.

_3	-3	3	3
GUIDED PRACTICE			10
Write an integer f	or each situation.		
4 . 6°F below 0	5 . a loss of 11	yards 6. a	a deposit of \$16
Evaluate each exp	ression.		
7 . 7	8. -4	9.	-7 - 1
10. STOCK MARKE days. Write an	T The price of a comp integer to represent th	any's stock fel e amount the s	l 21 points in two stock price fell.

CONTENTS

Practice and Applicatio	ns				
				HOMEW	ORK HELP
Write an integer for each situat	tion.			For Exercises	See Examples
11. a profit of \$9	12 . 53°C b	elow 0		11-18, 29	1, 2
13. no gain on first down	14. an elev	vator goes up 12 floors		19–22, 27, 28 23–26	3
15. 2008 A.D.	16 . 160 fee	t above sea level		Extra	Practice
17 . a bank withdrawal of \$50	18 . 1000 в.	С.		See page	5 309, 390.
Evaluate each expression.					
19. 6 20. -1	2	21 . -9	22.	21	
23. 12 - -8 24. -1	0 - 5	25. -9 + 5	26.	26 +	-4
27 . What is the absolute value of	of 0?	28. Find $ x $ if $x = -$	-6.		
29. STATIC ELECTRICITY Electri protons and negatively-charge through your hair to make the on the wall and 5 electrons of the wall and 5 e	cal charges are ged electrons. he balloon stick n the balloon.	e made up of positively Suppose you rub a ball k to a wall. There are 2 Write an integer for eac	-charge oon protons ch charg	ed 6 ge.	
Graph each set of integers on a	a number line				
30. {0, 1, -3} 31. {-4	, 5, 4}	32 . {-5, -1, 10, -9}	33.	{-2, -4,	-6, -8}
34. WEATHER A meteorologist yesterday to today. Describe	reports a 20° o what this co	change in the temperat uld mean.	ture fro	om	
CRITICAL THINKING Determin	ne whether ea	ch statement is <i>true</i> or	false.		

If *false*, give a counterexample.

- **35**. Every integer has an absolute value.
- 36. The absolute value of every integer is positive.



The mean income for a group of accountants is \$36,266.67. Their incomes are \$27,500, \$36,100, \$29,800, \$33,400, \$31,300, and \$59,500.

39. In what way is the mean misleading? (Lesson 2-8)

40. Draw a bar graph of the data. (Lesson 2-7)

GETTING READY FOR THE NEXT LESSON

PREREQUISITE SKILL Replace each ● with < or > to make a true sentence. (Page 556)

41. 16 • 6 **42.** 2.3 • 3.2 **43.** 101 • 111 **44.** 87.3 • 83.7

45. 1,051 ● 1,015

msmath2.net/self check quiz



What You'll LEARN

Compare and order integers.

REVIEW Vocabulary

median: the middle number in an ordered data set (Lesson 2-4)

MATH Symbols

- < is less than
- > is greater than

Comparing and Ordering Integers

WHEN

am I ever going to use this?

WEATHER The Wind Chill Temperature Index table shows how cold air feels on human skin.

- What is the wind chill if there is a wind at 20 miles per hour and the temperature is 5°?
- 2. Which is colder, a temperature of 15° with a 20 mile-per-hour wind or a temperature of 10° with a 10 mile-per-hour wind?

WIND CHILL								
	Temperature (°F)							
15	10	5	0	-5				
7	1	-5	-11	-16				
3	-4	-10	-16	-22				
0	-7	-13	- 19	-26				
-2	-9	-15	-22	-29				
	V 15 7 3 0 -2	WIND Temp 15 10 7 1 3 -4 0 -7 -2 -9	WIND CHILL Temperature 15 10 5 7 1 -5 3 -4 -10 0 -7 -13 -2 -9 -15	UND CHILL Temperature (F) 15 10 5 0 7 1 -5 -11 3 -4 -10 -16 0 -7 -13 -19 -2 -9 -15 -22				

3. Graph both wind chills found in Exercise 2 on a number line.

When two numbers are graphed on a number line, the number to the left is always less than the number to the right. The number to the right is always greater than the number to the left.

Notea	bles"	Key Concept: Compare Integers
Model		0 1
Words	-4 is less than -2 .	-2 is greater than -4 .
Symbols	-4 < -2	-2>-4
	The symbol points to the les	ser number.

EXAMPLE Compare Integers

Replace the • with < or > to make -5 • -3 a true sentence.

Graph each integer on a number line.

CONTENTS

- 1	-	1		1	1	1	1		1	1	1	1	
													-
-6	-5	-4	-3	-2	-1	0	1	2	3	4	5	6	
Since	-5	is to	the	left	of -3	3. –!	5 < -	-3					

Your Turn Replace each ● with < or > to make a true sentence.

```
a. -8 \bullet -4 b. 5 \bullet -1 c. -10 \bullet -13
```

READING in the Content Area

For strategies in reading this lesson, visit **msmath2.net/reading.**

smsmath2.net/extra_examples

Integers are used to compare numbers in many real-life situations.

CEN CEN Standardized-**Test Practice**

Test-Taking Tip

Choices

Eliminating Answer

If you are unsure of the

correct answer, eliminate

the choices you know are incorrect. Then consider

the remaining choices. You can eliminate choice C

since the list begins with a positive number.

EXAMPLE Order Integers

MULTIPLE-CHOICE TEST ITEM The lowest temperatures in Alaska, Florida, Hawaii, and Montana are listed in the table. Order the temperatures from least to greatest.

▲ -80, -70, 12, -2 **■** -80, -70, -2, 12 C 12, −2, −70, −80

● -2, 12, -70, -80

Record Low State **Temperature (°F)** Alaska -80 Florida -2 Hawaii 12 Montana -70

Source: The World Almanac and Book of Facts

Read the Test Item To order the integers, graph them on a number line. Solve the Test Item



Order the integers from least to greatest by reading from left to right: -80, -70, -2, 12. So, the answer is B.

Skill and Concept Check

- **1**. **Draw** a number line to show that -5 is less than -1.
- 2. **OPEN ENDED** Write an integer that is less than −9. Explain.
- **3. NUMBER SENSE** Complete the sentence: -7 is greater than -12 because -7 lies to the <u>?</u> of -12 on a number line.
- 4. Name the greatest negative integer.

GUIDED PRACTICE

Replace each ● with < or > to make a true sentence.

5. −5 • −6 **6**. −2 ● 8 **7.** 0 ● -10

8. Order 51, -63, 49, -24, -38, and 38 from least to greatest.

MONEY For Exercises 9 and 10, use the information below and at the right.

Marva is saving money for a new bike and has already saved \$21. She begins a log to keep track of her money.

- 9. Write each entry as an integer.
- **10**. Order the integers from least to greatest.

Money Log earned \$15 raking leaves -loaned \$13 to a friend -received allowance of \$10 spent\$4 on snacks friend paid back \$13 loan bought \$5 lunch



Practice and Applications

Replace each ● with < or > to make a true sentence.

11 . −17 • −20	12 . −21 • −12	13 . 3 ● −10	14 . −5 • 17
15. 4 ● −4	16. −25 • −20	17 . −52 • −72	18. 100 ● −10
19 . −8 ● 0		20 . −13 • −14	
21 . 36 ● −37		22 . −29 • 92	

Determine whether each sentence is *true* or *false*. If *false*, change one number to make the sentence true.

23.	-8 > 5	24. -7 < 0	25.	-9	= 9
26.	5 < -6	27. $10 > -8 $	28. 7	>	-7

WEATHER For Exercises 29 and 30, use the information in the table. It shows the record low temperatures in Indianapolis, Indiana, for March 1–7 of a recent year.

29. Arrange the dates from the coldest temperature to the warmest.

- **30**. Find the median temperature.
- **31**. Order -7, 5, -6, -4, 1, and 3 from least to greatest.
- **32**. Order |51|, -53, |-52|, 55, -56, and -57 from greatest to least.
- **33. CRITICAL THINKING** If 0 is the greatest integer in a set of five integers, what can you conclude about the other four integers?

Day	Temperature (°F)
Mar. 1	-4
Mar. 2	-7
Mar. 3	1
Mar. 4	3
Mar. 5	-1
Mar. 6	-6
Mar. 7	6

Source: www.weather.com

Year

1000 B.C.

1902 A.D.

600 A.D.

2000 B.C.

Toy

Teddy Bear

Yo-Yo

Chess

Checkers

Pa Review with Standardized Test Practice

- 34. **MULTIPLE CHOICE** The table shows the inventions of several toys. Order the inventions from earliest to most recent.
 - (A) chess, yo-yo, teddy bear, checkers
 - Checkers, yo-yo, chess, teddy bear
 - yo-yo, teddy bear, checkers, chess
 - D chess, teddy bear, yo-yo, checkers
- **35. GRID IN** Which is greater, -12 or 7?

Write an integer for each situation. (Lesson 3-1)

36. 9°C below 0

37.	а	gain	of	20	feet
-----	---	------	----	----	------

38. PROFITS The daily profits of T-shirts sold last week were \$55, \$35, \$25, \$30, and \$55. Which average might be misleading: the mode, the median, or the mean? Explain. (Lesson 2-8)

GETTING READY FOR THE NEXT LESSON

PREREQUISITE SKILL Graph the solution of each equation on a number line. (Lesson 1-5)

CONTENTS

39. x + 3 = 5**40.** x - 4 = 8

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41. 3x = 9**42.** 5x = 30

For Exercises	See Examples			
11-28	1			
29, 31–32	2			
Extra Practice See pages 570, 598.				

HOMEWORK HELP

Lesson 3-2 Comparing and Ordering Integers 111

What You'll LEARN

Graph points on a coordinate plane.

NEW Vocabulary

coordinate plane coordinate grid x-axis y-axis origin ordered pair x-coordinate y-coordinate quadrant

Geometry: The Coordinate Plane

WHEN am I ever going to use this?

MAPS A map of Terrell's neighborhood is shown.

- Suppose Terrell starts at the corner of Russel and Main and walks 1 block north and 2 blocks east. Name the intersection of his location.
- 2. Using the words *north, south, west,* and *east,* write directions to go from the corner of School and Highland to the corner of Main and Oak.



A **coordinate plane** is used to locate points. It is a plane in which a horizontal number line and a vertical number line intersect at their zero points. A coordinate plane is also called a **coordinate grid**.



An **ordered pair** is a pair of numbers such as (5, -2) used to locate a point in the coordinate plane.



EXAMPLE Name an Ordered Pair

Name the ordered pair for point *P*.

- Start at the origin.
- Move left to find the *x*-coordinate of point *P*, which is -4.
- Move up to find the *y*-coordinate, which is 2.

So, the ordered pair for point *P* is (-4, 2).





Graphing Moving right or up on a coordinate plane is in the *positive direction*. Moving left or down is in the *negative direction*.



READING Math

Scale When no numbers are shown on the *x*- or *y*-axis, you can assume that each grid is 1 unit long on each side.

EXAMPLE Graph an Ordered Pair

Graph and label the point Q(2, -5).

- Draw a coordinate plane.
- Move 2 units to the right. Then move 5 units down.
- Draw a dot and label it Q(2, -5).



Your Turn Graph each point.

a. A(6, 0)

b. B(-5, -3)

The coordinate plane is separated into four sections called **quadrants**.



Axes is the plural form of axis. The axes are not located in any of the quadrants.

LIFE CAREERS

How Does a Cartographer Use Math?

Cartographers use coordinates to prepare geographic, political, and cultural maps of large areas.



EXAMPLES Identify Quadrants

CONTENTS

GEOGRAPHY The world map can be divided into a coordinate grid where (x, y) represents (degrees longitude, degrees latitude). In which quadrant is the United States located?



The United States is located in the upper left quadrant, quadrant II.

Name a country from the map that is located in quadrant III. Quadrant III is the bottom-left quadrant. So, Chile is in quadrant III.



msmath2.net/extra_examples

- 1. Writing Mathe Explain why point A(1,-2) is different from point B(-2, 1).
- 2. **OPEN ENDED** Name and graph a point in quadrant IV.

GUIDED PRACTICE

Name the ordered pair for each point graphed at the right. Then identify the quadrant in which each point lies.

3. *P* **4**. *Q* **5**. *R*

On graph paper, draw a coordinate plane. Then graph and label each point.

6.	<i>S</i> (2, 3)	7 . <i>T</i> (-4, 6)	8 . <i>U</i> (−5, 0)
----	-----------------	-----------------------------	-----------------------------



Practice and Applications

Name the ordered pair for each point graphed at the right. Then identify the quadrant in which each point lies.

9 . A	10 . <i>B</i>
11 . C	12. D
13. E	14. <i>F</i>
15 . G	16 . <i>H</i>
17. I	18. <i> </i>





19. Write the ordered pair for the point that lies on the *y*-axis and is 32 units down from the origin.

On graph paper, draw a coordinate plane. Then graph and label each point.

20. <i>M</i> (5, 6)	21 . N(-2, 10)	22 . <i>P</i> (7, -8)	23 . <i>Q</i> (3, 0)
24. <i>R</i> (-1, -7)	25 . <i>S</i> (0, 6)	26. <i>T</i> (-3, 7)	27 . U(5, −2)
28. V(8, 1)	29 . W(−5, −7)	30. <i>X</i> (1.5, -3)	31 . <i>Y</i> (-6.5, 6.5)

Determine whether each statement is *sometimes, always,* or *never* true. Explain or give a counterexample to support your answer.

- **32**. Both *x* and *y*-coordinates of a point in quadrant I are negative.
- **33**. The *x*-coordinate of a point that lies on the *x*-axis is negative.
- **34**. The *y*-coordinate of a point in quadrant IV is negative.

GEOGRAPHY For Exercises 35 and 36, use the map in Example 3.

- **35.** In what country is the point (105° longitude, 30° latitude) located?
- 36. Find an ordered pair that can represent the location of California.



For Exercises 37–41, use the map of the Brookfield Zoo.

- **37.** What exhibit is located at (4, -2)?
- **38.** In which quadrant is the Dragonfly Marsh exhibit located?
- **39**. Find the ordered pair that represents the location of Baboon Island.
- **40**. What is located at the origin?



Source: www.brookfieldzoo.org

- **41**. Describe how you would walk from the entrance of the Pachyderm House at (-2, 2) to the entrance of The Swamp at (-1, -2).
- **42. GEOMETRY** Graph the points A(-3, 2), B(2, 2), C(2, -4), and D(-3, -4) on the same coordinate plane. Connect the points from A to B, B to C, C to D, and D to A. Name the figure.
- **43. CRITICAL THINKING** Find the possible locations for any ordered pair whose *x* and *y*-coordinates are always the same integer. Explain.





Mid-Chapter Practice Test

Vocabulary and Concepts

CHAPTER

- 1. **Define** *absolute value*. (Lesson 3-1)
- 2. Write the ordered pair which identifies a point 4 units to the left of the *y*-axis and three units above the *x*-axis. (Lesson 3-3)
- 3. Draw a coordinate plane, and label the quadrants. (Lesson 3-3)

Skills and Applications

Write an integer for each situation. (Lesson 3-1)

- **4.** 45 feet below sea level**5.** a deposit of \$100
- **6**. a gain of 8 yards **7**. lost a \$5 bill

Replace each • with < or > to make a true sentence. (Lesson 3-2)

- **8.** $-12 \bullet -9$ **9.** $-4 \bullet 4$ **10.** $|-14| \bullet |3|$
- **11. FOOTBALL** The Tigers have recorded the following yardage on the past six plays: 9, -2, 5, 0, 12, and -7. Order the integers from least to greatest. (Lesson 3-2)

On graph paper, draw a coordinate plane. Then graph and label each point. (Lesson 3-3)

12. D(4, -3) **13.** E(1, 3) **14.** F(0, -5)

Standardized Test Practice

 MULTIPLE CHOICE Which of the following points represents a number and its absolute value? (Lesson 3-1)

$$A B C D E F$$

$$-4 -3 -2 -1 0 1 2 3 4$$

$$B and E B C and F$$

- \bigcirc *B* and *D* \bigcirc *A* and *E*
- **16. SHORT RESPONSE** The table shows the number of inches of monthly precipitation above or below normal for a midwestern city in a recent year. Find the median monthly precipitation above or below normal. (Lesson 3-2)

Monthly Precipitation Above or Below Normal					
J	F	Μ	Α	Μ	J
4	-1	6	-2	-3	1
J	A	S	0	Ν	D
-2	-1	2	-3	1	-3

A Place To Practice your Math Skills

Tic-Tac-Toe

GETREADY

Players: two Materials: grid paper

GET SETI

- Draw a coordinate plane on grid paper.
- This game is similar to tic-tac-toe, except players must get four Xs or four Os in a row.

• GO!

- Player 1 chooses two numbers: the first number is the x-coordinate of an ordered pair, and the second number is the y-coordinate. Each number must be between -5 and 5. Then Player 1 announces the ordered pair and plots the X or O on the coordinate plane.
- Player 2 then chooses his or her numbers, announces them, and plots the points.
- An ordered pair cannot be changed after it has been announced.
- If a player announces an ordered pair that has already been used or graphs an ordered pair incorrectly, the player loses a turn.
- Who Wins? The first player to get four Xs or Os in a row is the winner.



Graphing Points on a Coordinate Plane

HANDS-ON LAB

A Preview of Lesson 3-4



• You can add or remove zero pairs from a mat because adding or removing zero does not change the value of the counters on the mat.

You will use zero pairs in Activity 2 and Activity 3.







CONTENTS

- 1. Write two addition sentences where the sum is positive. In each sentence, one addend should be positive and the other negative.
- **2**. **Write** two addition sentences where the sum is negative. In each sentence, one addend should be positive and the other negative.
- **3. MAKE A CONJECTURE** Write a rule that will help you determine the sign when finding the sum of integers.

What You'll LEARN

Add integers.

NEW Vocabulary

opposites additive inverse

Link to READING

Everyday Meaning of Opposite: something that is across from or is facing the other way, as in running the opposite way

Adding Integers

MHEN am I ever going to use this?

EARTH SCIENCE Thunderstorms are made of both positive and negative electrical charges. The negative charges (electrons) are at the bottom of a thundercloud, and positive charges (protons) are at the top.

1. What is the charge at the top of a cloud where there are more protons than electrons?



2. What is the charge at the bottom of a cloud where there are more electrons than protons?

Combining positive and negative electrical charges in a thunderstorm is similar to adding integers.

EXAMPLE Add Integers with the Same Sign

Find -3 + (-2).

Use a number line.

- Start at 0.
- Move 3 units left to show -3.
- From there, move 2 units left to show -2.

So, -3 + (-2) = -5.



Noteables Key Concept: Add Integers with the Same Sign

Words The sum of two positive integers is positive.

The sum of two negative integers is negative.

Examples 7 + 4 = 11 -7 + (-4) = -11

EXAMPLE Add Integers with the Same Sign Find -26 + (-17). -26 + (-17) = -43 The sum of two negative integers is negative.

a. -14 + (-16) b. 23 + 38

c. -35 + (-49)



Richard Kaylin/Getty Images



The integers 43 and -43 are called **opposites** of each other because they are the same distance from 0, but on opposite sides of 0. Two integers that are opposites are also called **additive inverses**.





CONTENTS

d. 10 + (-12) e. -16 + 9 f. -13 + 18

EXAMPLE Simplify an Expression with Integers

ALGEBRA Simplify 12 + x + (-20).

12 + x + (-20) = 12 + (-20) + x Commutative Property of Addition = -8 + x Add.

Your Turn Simplify each expression.

g. 1 + y + (-5)

h. z + (-2) + 9

REAL-LIFE MATH

OCEANOGRAPHY The Great Barrier Reef off the coast of Australia is home to 1,500 species of fish and 215 species of birds.

Source: www.ozramp.net.au



EXAMPLE Use Integers to Solve a Problem

OCEANOGRAPHY Anna was scuba diving near the Great Barrier Reef 16 meters below the surface of the water. She saw a dolphin swim by 7 meters above her. What was the depth of the dolphin?

Anna is 16 meters underwater, and the dolphin is 7 meters above her. So, the depth of the dolphin can be represented by the expression -16 + 7, or -9.

The dolphin is 9 meters below the surface of the water.

Skill and Concept Check

- **1. Draw** a model to show 2 + (-7).
- 2. **OPEN ENDED** Give an example of integers that are additive inverses.
- **3. FIND THE ERROR** Brooke and Javier are finding -12 + 13. Who is correct? Explain.

Brooke Javier -12 + 13 = 1 -12 + 13 = -1

4. **NUMBER SENSE** Tell whether each sum is *positive*, *negative*, or *zero* without adding.

a. -6 + (-7) **b.** -8 + 10 **c.** -14 + 14

GUIDED PRACTICE

Add.

- **5.** -6 + (-8) **6.** -3 + 10 **7.** 7 + (-11) **8.** 9 + (-9)
- **9. MONEY** You pay your brother \$42 that you owe him. The same week you earn \$35 dog-sitting for the neighbors. Do you have more or less money than at the beginning of the week?
- **10. ALGEBRA** Simplify 12 + y + (-8).



Practice and Applications

		HOMEW	UK
Add.		For Exercises	s Se
11. -8 + 8 12. -9	+ 11 13. $13 + (-19)$ 14. $6 + 10$	11-42	
15 -10 + (-15) 16 -1	2 + 10 17 $-30 + 16$ 18 $18 + (-5)$	46–57	
	2 + 10 II . $30 + 10$ II . $10 + (-3)$	43-45, 58	
19. 21 + (-21) 20. 18	+ (-20) 21 . $-22 + (-16)$ 22 . $-24 + 19$	Extra See pag	Praces 57
23. $-11 + 13 + 6$	24. $-16 + (-21) + 15$		
25. 12 + (-17) + (-25)	26. $20 + (-30) + (-40)$		

Write an addition expression to describe each situation. Then find each sum.

- **27.** WEATHER The temperature outside is -3° F. The temperature drops 6° .
- 28. **SUBMARINE** A submarine dives 106 feet below the water. Then, it rises 63 feet.
- 29. SKATEBOARDING Hakeem starts at the bottom of a half pipe 6 feet below street level. He rises 14 feet at the top of his kickturn.
- **30. MONEY MATTERS** Stephanie has \$43 in the bank. She withdraws \$35.

ALGEBRA Evaluate each expression if x = -10, y = 7, and z = -8.

31. <i>x</i> + 14	32. $6 + y$	33. <i>z</i> + (-5)	34 . −17 + <i>y</i>
35. 20 + z	36. $-10 + x$	37. <i>z</i> + 8	38. 15 + x
39. $x + y$	40. $y + z$	41. $x + z$	42. $x + y + z$

GOLF For Exercises 43–45, use the information below.

Scores over par in a golf tournament are recorded as positive integers. Scores under par are recorded as negative integers. Even par is recorded as 0. The person with the lowest total score wins. The table shows the top two finishers in the 2004 LPGA Championship.

- 43. Find Annika Sorenstam's final score.
- 44. Find Shi Hyun Ahn's final score.
- **45**. Who had the better score? Explain.

	Round 1	Round 2	Round 3	Round 4
Annika Sorenstam	-3	-4	-7	+1
Shi Hyun Ahn	-2	-1	-2	-5

Source: www.lpga.com

Data Update What were the four-round scores of the latest winners of the LPGA Championship? Visit msmath2.net/data_update to learn more.

ALGEBRA Simplify.

46.	x + (-5) + 1
49.	8 + (-8) + n

47. 4 + y + (-2)**50.** -1 + a + 7

48. -9 + m + (-6)**51.** f + (-19) + 11

msmath2.net/self check quiz



Lesson 3-4 Adding Integers 123 Tony Feder/Getty Images

HOMEWOR K HE

Explain how the Commutative and Associative Properties of Addition can help you find each sum mentally. Then find each sum.

- **52.** 7 + (-2) + (-7)**53.** -6 + 9 + (-4)**54.** -5 + (-6) + (-3)**55.** 8 + 10 + (-8)**56.** -5 + (-7) + (-10)**57.** 8 + (-9) + 9
- **58. STOCK MARKET** The members of the Investment Club purchased a stock for \$50. The next day the price of the stock dropped \$18. On the second and third days, the price dropped another \$16 and then rose \$21. How much was the stock worth at the end of the third day?
- **59. WRITE A PROBLEM** Write about a real-life problem using the addition sentence -8 + 11 = t. Then solve the equation and explain what the solution represents.

CRITICAL THINKING For Exercises 60 and 61, use a number line to find each sum. Does the order of the addends make a difference? Explain.

60. 3 + (-8) and -8 + 3

61. [7 + (-3)] + (-6) and 7 + [-3 + (-6)]

Spiral Review with Standardized Test Practice

62. MULTIPLE CHOICE In a game with a standard deck of cards and the scoring system at the right, three cards are dealt and added together to get a final score. Dylan is dealt the 4 of hearts, the king of spades, and the 3 of diamonds. What is his final score?



63. SHORT RESPONSE Jeremy owes his sister \$5. Then he borrows \$6 more from her. Write the total amount he owes as an integer.

D 9

Name the ordered pair for each point graphed at the right. Then identify the quadrant in which each point lies. (Lesson 3-3)

C 3

64.	J	65.	Κ
66.	L	67.	М

B -3

- **68**. Order 6, -3, 0, 4, -8, 1, and -4 from least to greatest. (Lesson 3-2)
- **69. STATISTICS** Construct a line plot for the following test scores: 81, 83, 75, 81, 82, 81, 75, 82, 82, 86, 83, 81, and 79. (Lesson 2-3)

GETTING READY FOR THE NEXT LESSON

PREREQUISITE SKILL Find the range for each set of data. (Lesson 2-3)

70. 13, 7, 6, 22, 21

▲ -11

71. 54, 32, 43, 49, 30

72. 62, 59, 85, 74, 82

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Use a Flowchart

Taking Good Notes

Have you ever tried to solve a math problem and then realized you left out an important step? Try using a flowchart when you take notes to map out the steps you should follow. A *flowchart* is like a map that tells you how to get from the beginning of a problem to the end.



Here's a flowchart for adding two integers. Just follow the arrows.



SKILL PRACTICE

Make a flowchart for each kind of problem.

- 1. rounding a decimal to a given place (See page 557.)
- 2. evaluating an expression using order of operations (See Lesson 1-3.)



HANDS-ON LAB

A Preview of Lesson 3-5

What You'll LEARN

Use counters to model the subtraction of integers.

_	_	_	_	_
_				
_	610	11 1		-
		2161		S

- counters
- integer mat



You can also use counters to model subtraction of integers. Remember one meaning of subtraction is to *take away*.



CONTENTS



Writing Math

CONTENTS

Work with a partner.

- 1. Write two subtraction sentences where the difference is positive. Make sure you use a combination of positive and negative integers.
- **2. Write** two subtraction sentences where the difference is negative. Make sure you use a combination of positive and negative integers.
- **3. MAKE A CONJECTURE** Write a rule that will help you determine the sign of the difference of two integers.

READING Math

Minuends, Subtrahends, and Differences In the subtraction sentence -4 - 3 = -7, -4 is the minuend, 3 is the subtrahend, and -7 is the difference.

Subtracting Integers



When you subtract 5, as shown in the Mini Lab, the result is the same as adding -5. When you subtract 4, the result is the same as adding -4.



EXAMPLES Subtract Positive Integers Subtract. 8 - 13 8 - 13 8 - 13 = 8 + (-13) To subtract 13, add -13. = -5 Simplify. -10 - 7 -10 - 7 -10 - 7 = -10 + (-7) To subtract 7, add -7. = -17 Simplify.

CONTENTS

EXAMPLES Subtract Negative Integers Find 1 − (−2). 1 - (-2) = 1 + 2To subtract -2, add 2. = 3Simplify. Find -10 - (-7). -10 - (-7) = -10 + 7 To subtract -7, add 7. = -3 Simplify. Your Turn Subtract. a. 4 - (-12) b. -15 - (-5) c. 18 - (-6)





EXAMPLE Use Integers to Solve a Problem

EARTH SCIENCE

The legend on the sea-surface temperature map shows the minimum temperature at −2°C and the maximum temperature at 31°C. What is the range of temperatures on the map?



To find the range, or difference in temperatures, subtract the lowest temperature from the highest temperature.

31 - (-2) = 31 + 2 To subtract -2, add 2. = 33Simplify. So, the range of temperatures is 33°C.



Technology Use

the ____ key to subtract a number. Use the (-) key to enter a negative number.

msmath2.net/extra examples



Skill and Concept Check

- 1. Writing Mathe Explain how additive inverses are used in subtraction.
- **2. OPEN ENDED** Write a subtraction sentence using integers. Then, write the equivalent addition sentence and find the sum.
- **3. FIND THE ERROR** Bradley and Mitsu are finding -16 (-19). Who is correct? Explain.

GUIDED PRACTICE

Subtract.

4. -4 - 8 **5.** 14 - 17 **6.** 14 - (-10) **7.** -3 - (-1)

ALGEBRA Evaluate each expression if p = 8, q = -14, and r = -6.

8. p - q 9. q - r 10. r - p

11. METEOROLOGY The highest temperature ever recorded on Earth was 136°F in Libya. The lowest temperature was -129°F in Antarctica. What is the range of the highest and lowest temperatures on Earth?

Practice and Applications

Subtract.

				I UI LACICISES	See Examples
12.	-9 - 5	13. 0 - 10	14 8 - 9	12-31	1–4
15	17 _ 13	16 $27 - (-8)$	17 - 25 - (-5)	32-44	5
15.	17 15	18. 27 (8)	17.23(3)	45-48	6
18.	12 - 26	19. $4 - (-19)$	20 11 - 42	Extra I	Practice
24		22 27 (10)	10 (00)	See page	\$ 571, 598.
21.	15 - (-14)	22 . $-27 - (-19)$	23 . $-18 - (-20)$		
24.	31 - 48	25 33 - (-27)	26. 52 - (-52)		
27.	-44 - (-41)	28. $-2 - 9 + 7$	29. $6 + (-1) - 4$		

30. What is -3 minus 4?

31. Find -23 - (-19).

HOMEWORK HELP

For Evorcicos Soo Evampla

ALGEBRA Evaluate each expression if f = -6, g = 7, and h = 9.

32. 5 – <i>f</i>	33. <i>h</i> - (-9)	34. <i>f</i> − <i>g</i>	35 . <i>g</i> - 7
36. <i>h</i> - <i>f</i>	37. <i>f</i> – 6	38. <i>g</i> – <i>h</i>	39 . 4 - (- <i>g</i>)
40. − <i>h</i> − 10	41. $-f - h$	42. $f - g - h$	43. <i>h</i> − <i>g</i> − <i>f</i>

44. ALGEBRA Find |a - b| when a = -7 and b = 11.

45. GEOGRAPHY The Dead Sea's deepest part is 799 meters below sea level. A plateau to the east of the Dead Sea rises to about 1,340 meters above sea level. What is the difference between the deepest part of the Dead Sea and the top of the plateau?



HISTORY For Exercises 46–48, use the timeline that shows the lives of three rulers of Rome.



- 46. How old was Augustus when he died?
- 47. Who lived the longest? How old was he when he died?
- **48**. How many years were there between when Julius Caesar was born and when Tiberius died?

Determine whether each statement is *sometimes, always,* or *never* true. Give an example or counterexample for each answer.

- **49**. negative positive = negative **50**. negative negative = positive
- **51.** positive positive = positive = negative =

53. CRITICAL THINKING

True or *False*? When *n* is a negative integer, n - n = 0.

pjra Review with Standardized Test Practice 🏒

54. MULTIPLE CHOICE Find the correct subtraction sentence shown in the model.



55. SHORT RESPONSE The temperatures on the moon vary from -173° C to 127°C. Find the range of temperatures.

Add. (Lesson 3-4)

56.
$$10 + (-3)$$
 57. $-2 + (-9)$ **58.** $-7 + (-6)$ **59.** $-18 + 4$

60. In which quadrant do ordered pairs with a positive *x*-coordinate and a negative *y*-coordinate lie? (Lesson 3-3)

GETTING READY	FOR THE NEXT LESSO	N I	
BASIC SKILL M	ultiply.		
61 . 14 · 5	62. 9 · 16	63 . 6 · 8 · 4	64. 11 · 7 · 7
msmath2.net/se	elf_check_quiz		Lesson 3-5 Subtracting Integers 131
			Richard T. Nowitz/Getty Images



What You'll LEARN

Solve problems using the look for a pattern strategy.

Problem-Solving Strategy A Preview of Lesson 3-6

Look for a Pattern

We've already saved \$155 in four months. If we keep saving our money at the same rate, how long do you think it will take to save enough money to buy a DVD player that costs \$330?

I found the table where we listed our savings each month. Let's **look for a pattern** to figure it out.

Explore	We began with \$50 and added more money to our savings every month. We need to find the number of months when we will have \$330 to buy the DVD player.
Plan	Let's look for a pattern or rule that increases the balance each month. Then use the rule to extend the pattern and find the solution.
Solve	After the initial \$50, we saved \$35 per month. To extend the pattern, add \$35 to each monthly balance until the balance equals \$330. We will have enough money saved after 9 months.
Examine	We saved about $2 \times $ \$155, or \$310 in 8 months. So, 9 months is a reasonable answer.

Month	Balance
1	\$50
2	\$85
3	\$120
4	\$155

Month	Balance
1	\$50
2	\$85
3	\$120
4	\$155
5	\$190
6	\$225
7	\$260
8	\$295
9	\$330

Analyze the Strategy

- **1. Explain** when you would use the look for a pattern strategy to solve a problem.
- **2. Describe** how to solve a problem using the look for a pattern method as a problem-solving strategy.
- **3.** Write a problem that could be solved by looking for a pattern. Explain your answer.
- **132** Chapter 3 Algebra: Integers John Evans



Apply the Strategy

Solve. Use the look for a pattern strategy.

4. **LIFE SCIENCE** The table shows about how many times a firefly flashes at different

temperatures.		
Estimate how		
many times		
a firefly will		
flash when the		
temperature		
is 36°C.		

Outside Temperature (°C)	Flashes per Minute
16	8
20	9
24	11
28	14

Mixed Problem Solving

Solve. Use any strategy.

LIFE SCIENCE For Exercises 6–8, use the information and the graph.

- 6. What does 0 on this graph represent?
- Write an integer to represent the rainfall for each month.



- 8. Write a sentence that summarizes the message this graph conveys about this summer's rainfall.
- **9. EARTH SCIENCE** Hydrothermal vents are similar to geysers, but are found on the ocean floor. A hydrothermal vent chimney can grow at an average rate of 9 meters in 18 months. What is the average rate of growth per month?
- **10. MULTI STEP** Francisco is on vacation and is planning to send postcards and letters to his friends. He has \$3.04 to spend on postage. A stamp for a letter costs 37¢, and a stamp for a postcard costs 23¢. If he is going to spend the entire \$3.04 on postage, how many postcards and letters can he send?

5. **CEREAL** A display of cereal boxes is stacked in the shape of a pyramid. There are 4 boxes in the top row, 6 boxes in the second row, 8 boxes in the next row, and so on. The display contains 7 rows of boxes. How many boxes are in the display?

- **11. BASKETBALL** Laura makes 3 free throws out of every 5 she attempts. Find the number of free throws she will make after 15, 20, and 30 attempts.
- **12. COINS** Olivia has seven coins that total \$1.32. What are the coins?
- FOOD The school cafeteria added a breakfast special to their menu. The table shows the foods that are part of the special and the number of Calories. Estimate how many Calories there are in the special.

Food	Calories
whole-wheat bagel	156
skim milk	90
nonfat strawberry yogurt	183
fresh fruit salad	68

14. STANDARDIZED TEST PRACTICE

CONTENTS

The total land area of Illinois is about 55,593 square miles. According to the 2000 U.S. Census Bureau, about 223.4 persons per square mile were living in Illinois. What was the approximate population of Illinois in 2000?

A 124,000	B 1,240,000
C 12,400,000	D 124,000,000

Lesson 3-6a Problem-Solving Strategy: Look for a Pattern 133

Multiplying Integers



Remember that multiplication is the same as repeated addition. The multiplication expression 4(-2) in the Mini Lab means that -2 is used as an addend four times.

$$4(-2) = (-2) + (-2) + (-2) + (-2)$$

$$= -8$$

$$-8 -7 -6 -5 -4 -3 -2 -1 0 1$$

By the Commutative Property of Multiplication, 4(-2) = -2(4). When two integers have different signs, the following rule applies.

Noteal	iles"	Key Conce	pt: Multiply Integers with Different Signs
Words	The pr	oduct of two	integers with different signs is negative.
Examples	6(-4)	= -24	-5(7) = -35

EXAMPLES Multiply Integers with Different Signs







Zero The

Multiplicative Property of Zero states that when any number is multiplied by zero, the product is zero. The product of two positive integers is positive. You can use a pattern to find the sign of the product of two negative integers.



When two integers have the same sign, the following rule applies.

Key Concept: Multiply Integers with Same SignWordsThe product of two integers with the same sign is positive.Examples2(6) = 12-10(-6) = 60



EXAMPLES Simplify and Evaluate Expressions

ALGEBRA Simplify -2(3x).
-2(3x) = (-2 · 3)x Associative Property of Multiplication = -6x Simplify.
ALGEBRA Evaluate pqr if p = -3, q = 4, and r = -1. pqr = (-3)(4)(-1) Replace p with -3, q with 4, and r with -1. = (-12)(-1) Multiply -3 and 4. = 12 Multiply -12 and -1.
Your Turn
d. Simplify -5(2y).
e. Evaluate xyz if x = -7, y = -4, and z = 2.

CONTENTS



review exponents in Lesson 1-2.



msmath2.net/extra_examples

Skill and Concept Check

- 1. Model the product of 2 and -3 using counters. Then write the multiplication sentence.
- 2. **OPEN ENDED** Name two integers whose product is negative.
- 3. **NUMBER SENSE** What is the sign of the product of three negative integers? Give an example.

GUIDED PRACTIN	CE			1.1	
Multiply.					
4. 6(-10)	5 15(-3	6 .	$(-2)^2$		
ALGEBRA Simp	lify each expressior	ı.			
7 5(2 <i>a</i>)	8. 3(-6b)	9.	-5(-9 <i>c</i>)		
ALGEBRA Evalu	ate each expression	if $f = -1, g = 7$,	and $h = -10$.		
10 . 5 <i>f</i>	11 . <i>fgh</i>	12.	$-h^{2}$		
13. SUBMARINE a rate of 125 7 minutes?	S A submarine is di feet per minute. Wh	iving from the sur at is the depth of	face of the wate the submarine a	er at After	
Practice and	Applications			HONEY	
Multiply.				For Evercise	
14. 8(-13)	15 16(-5)	16. $(-9)^2$	17 10(-17	7) 14–27, 44	1-4
18. -7(16)	19. $(-6)^2$	20 20(-8)	21 15(30)	28–35 36–43	5
22 31(-5)	23 . 11(-20)	24. $-(7^2)$	25 . $(-4)^3$	Extra See pag	a Practice ges 571, 598.
26 . Find the prod	duct of -13 and 13 .	27 . Fin	d -7 squared.		
ALGEBRA Simp	lify each expressior	ı.			
28. -3(6 <i>c</i>)	29. -7(10 <i>d</i>)	30. 5(-	-4e)	31. 9(-8f)	
32. $-2(-3g)$	33 6(-4 <i>h</i>)	34. (2 <i>x</i>)(-3 <i>y</i>)	35. (-5 <i>r</i>)(2 <i>s</i>)	;)
ALGEBRA Evalu	ate each expression	if $w = 7, x = -8$, <i>y</i> = 5, and <i>z</i> =	10.	
36. $-4w$	37. <i>xy</i>	38. -2	XZ	39. <i>xyz</i>	
40 . −7 <i>wy</i>	41. $-3z^2$	42. 12 <i>x</i>	²	43. $-wz^2$	
44. VOLUNTEER citizens' hom could remove represent the in five hours	NG The Volunteer (les in the neighborhore 8 cubic meters of lo number of cubic mo	Club raked leaves ood. If each group eaves in one hour, eters of leaves 12	at several senio of three studen , find an integer students could r	r its to remove	

45. PATTERNS Find the next two numbers in the pattern 1, -2, 4, -8, 16, ...Then describe the pattern.



GEOMETRY For Exercises 46–48, use the graph at the right.

- **46**. Name the ordered pairs for *P*, *Q*, and *R*. Multiply each *x* and *y*-coordinate by −1 to get three new ordered pairs.
- 47. Graph the ordered pairs and connect them to form a new triangle.47. Describe its position with respect to the original triangle.
- **48**. In which quadrant does a triangle lie if only the *y*-coordinates of the original triangle are multiplied by -2?
- **49. CRITICAL THINKING** For what values of *n* is $(-2)^n$ positive?

Spiral Review with Standardized Test Practice

- **50. MULTIPLE CHOICE** An oil rig is drilling into the ground at a rate of 7 feet per minute. What integer represents the position of the oil rig after 42 minutes?
 - (A) -294 ft (B) -35 ft (C) 35 ft (D) 294 ft
- **51. MULTIPLE CHOICE** Monifa has 100 shares of stock each worth \$15. If the price drops to \$8, what integer represents the change in Monifa's current investment?

(F) −\$700 (G) −\$7 (H) \$7 (1) \$700

- **52. GRID IN** Evaluate $-6[-2(3) + 0(-5)] + (-4)^2$.
- **53.** Find -25 (-33). (Lesson 3-5)

ALGEBRA Evaluate each expression if x = -4, y = 6, and z = 1. (Lesson 3-4)

54. x + (-2) **55.** -1 + z **56.** -15 + y **57.** x + y

CONTENTS

58. EARTH SCIENCE The low temperatures in degrees Fahrenheit for ten cities on January 23 were −3, 27, 13, −6, −14, 36, 47, 52, −2, and 0. Order these temperatures from greatest to least. (Lesson 3-2)

MILITARY For Exercises 59 and 60, use the double-bar graph at the right. (Lesson 2-7)

- **59.** In which age groups are there more members in the Navy than members in the Air Force?
- **60**. About how many 36–40 year olds are in the Air Force?



GETTING READY FOR THE NEXT LESSON

BASIC SKILL Divide.

msmath2.net/self check quiz

61. 72 ÷ 9

62. 120 ÷ 6

63. 84 ÷ 21

64. 215 ÷ 43

Lesson 3-6 Multiplying Integers 137

Tim Wright/CORBIS



Dividing Integers



Division of integers is related to multiplication. When finding the quotient of two integers, you can use a related multiplication sentence.



Since multiplication and division sentences are related, you can use them to find the quotient of integers with different signs.

$$8(-9) = -72 \rightarrow \boxed{-72 \div 8} = -9$$

$$-8(-9) = 72 \rightarrow \underbrace{72 \div (-8)}_{\text{different signs}} = -9$$

$$\boxed{\text{different signs}}$$

These related sentences lead to the following rule.





READING Math

Division Sentence In the division sentence $80 \div (-10) = -8$, 80 is called the *dividend*, -10 is called the *divisor*, and -8 is called the *quotient*.





The quotient of two integers with the same sign is positive.

Noteal	les"	Key	Concept: Divide Integers with the Same Sign
Words	The qu	uotient of	f two integers with the same sign is positive.
Examples	15 ÷ 5	i = 3	$-21 \div (-3) = 7$



ASTRONOMY In January 2004, Mars Exploration Rover successfully sent signals to Earth after landing on Mars.

REAL-LIFE MATH



EXAMPLE Evaluate an Expression

ASTRONOMY The average surface temperature on Mars is -81° F. Use the expression $\frac{5(F-32)}{9}$, where *F* represents the number of degrees Fahrenheit, to find the temperature on Mars in degrees Celsius.

 $\frac{5(F-32)}{9} = \frac{5(-81-32)}{9}$ Replace *F* with -81. $= \frac{5(-113)}{9}$ Subtract 32 from -81. $= \frac{-565}{9}$ Multiply 5 and -113. ≈ -62.8 Divide.

CONTENTS

The average temperature on the surface of Mars is about -63° C.



smsmath2.net/extra_examples

Skill and Concept Check

- 1. Write two division sentences related to the multiplication sentence $-6 \cdot 7 = -42$.
- **2. OPEN ENDED** Write a division sentence. Then draw a model to show how the quotient can be found.
- **3. Which One Doesn't Belong?** Identify the division expression whose quotient does not have the same sign as the other three. Explain your reasoning.

-24 ÷ 6	-18 ÷ (-9)	28 ÷ (-7)	-22 ÷ 11
GUIDED PRACTICE			10
Divide. 4. 32 ÷ (−8)	5 . −16 ÷ 2	6 . −60 ÷ (−5) 7 . −	$\frac{-6}{6}$
ALGEBRA Evaluat	e each expression i	f $d = -9$, $e = 36$, and $f = -9$	= -6.
8 . −108 ÷ <i>f</i>	9 . <i>e</i> ÷ <i>d</i>	10. $\frac{e-f}{f}$	

Practice and ApplicationsDivide.11. $-18 \div 9$ 12. $50 \div (-5)$ 13. $-15 \div (-3)$ 14. $\frac{21}{-7}$ 15. $56 \div (-8)$ 16. $\frac{0}{-5}$ 17. $-52 \div (-13)$ 18. $-34 \div 2$ 19. $\frac{90}{6}$ 20. $-300 \div 25$ 21. $99 \div (-99)$ 22. $-184 \div (-23)$

- **23**. Find the quotient of -65 and 13.
- **24**. Divide 200 by -100.

ALGEBRA Evaluate each expression if r = 12, s = -4, and t = -6.

25. $-12 \div r$	26. 72 ÷ <i>t</i>	27. <i>r</i> ÷ <i>s</i>	28. <i>rs</i> ÷ 16
29. $\frac{-r}{t}$	30. $\frac{16 - (-r)}{-s}$	31. $t^2 \div r$	32. $\frac{r^2}{s^2}$

- **33. FOOTBALL** During the fourth quarter, the Colts were penalized 3 times for the same amount for a total of 45 yards. Write a division sentence to represent this situation. Then find the number of yards for each penalty.
- 34. **EARTH SCIENCE** Use the expression $\frac{5(F-32)}{9}$, where *F* represents the number of degrees Fahrenheit, to convert 5°F to degrees Celsius.
- **35. PATTERNS** Find the next two numbers in the pattern 729, -243, 81, -27, 9, ... Explain your reasoning.



- **36. SALES** The graph shows five magazines that had losses in a recent year. The numbers represent the profit the magazines made in 2006 compared to 2005. What is the mean of the losses for these five magazines?
- **37. MULTI STEP** The sea otter population is increasing. There were 2,377 sea otters in 1995. The population rose to 2,505 in 2003. Find the average rate of change for the sea otter population between 1995 and 2003.



- **38. WRITE A PROBLEM** Write about a situation in your life in which you used positive and negative integers. Create a problem and solve it using any of the four operations.
- **39. CRITICAL THINKING** List all of the numbers by which -20 is divisible.



49. PHYSICAL SCIENCE A chemistry experiment requires 3 milligrams of potassium chloride. How many grams of potassium chloride are needed? (Lesson 1-8)



Study Guide and Review

Vocabulary and Concept Check

absolute value (p. 107) additive inverse (p. 121) coordinate grid (p. 112) coordinate plane (p. 112) graph (p. 106) integer (p. 106) negative integer (p. 106) opposite (p. 121) ordered pair (p. 112) origin (p. 112) positive integer (p. 106) quadrant (p. 113) x-axis (p. 112) x-coordinate (p. 112) y-axis (p. 112) y-coordinate (p. 112)

Choose the correct term or number to complete each sentence.

- 1. Integers less than zero are (positive, negative) integers.
- **2.** Two numbers represented by points that are the same distance from 0 are (opposites, integers).
- **3**. The absolute value of 7 is (7, -7).
- **4**. The opposite of (-12, 12) is -12.
- **5**. The (coordinate plane, origin) is the point where the horizontal and vertical number lines intersect.
- 6. The *x*-axis and the *y*-axis separate the plane into four (quadrants, coordinates).
- 7. The first number in an ordered pair is the (*x*-coordinate, *y*-coordinate).
- 8. The sum of two (positive, negative) integers is negative.
- 9. The product of a positive and a negative integer is (positive, negative).
- **10**. The quotient of a negative integer and a (positive, negative) integer is negative.

Lesson-by-Lesson Exercises and Examples

Integers and Absolute Value (pp. 106–108)

Write an integer for each situation.

- **11**. a loss of \$150
- **12**. 350 feet above sea level
- **13**. a gain of 8 yards
- **14**. 12°F below 0

Evaluate each expression.

- **15**. |-11|
- **16**. |100|
- 17. 5
- **18**. |-32|
- **19.** |-16| + |9|

Example 1 Write an integer for 8 feet below sea level.

Since this situation represents an elevation *below* sea level, -8 represents the situation.

Example 2 Evaluate |-10|.

On the number line, the graph of -10 is 10 units from 0.



So,
$$|-10| = 10$$

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Comparing and Ordering Integers (pp. 109–111)

Replace each ● with < or > to make a true sentence.

20 . −3 • −9	21 . 8 ● −12
22 . −3 • 3	23 . −10 ● −13
24 . 25 • 8	25 . 0 ● −4

Order each set of integers from least to greatest.

- **26.** -3, 8, -10, 0, 5, -12, 9 **27.** -21, 19, -23, 14, -32, 25
- **28**. |-17|, -18, 18, |15|, -16, |16|
- **29. EARTH SCIENCE** The predicted low temperatures for Monday through Friday are 3°, −1°, −2°, 0°, and 1°. Order the temperatures from greatest to least.

Example 3 Replace • with < or > to make $-4 \cdot -7$ a true sentence.

Graph each integer on a number line.

		1							
	•	1	1	•				1	1-
-8	-7	-6	-5	-4	-3	-2	-1	0	1

Since -4 is to the right of -7, -4 > -7.

Example 4 Order the integers -4, -3, 5, 3, 0, -2 from least to greatest.

Graph the integers on a number line.

_									_
- T	Τ.	Τ.	1	Τ.	1		T	1	-
-4	-3	-2	-1	0	1	2	3	4	5
	Ŭ	-		Ŭ	•	-	Ŭ	•	Ū

Order the integers by reading from left to right: -4, -3, -2, 0, 3, 5.

3 Geometry: The Coordinate Plane (pp. 112–115)

Name the ordered pair for each point graphed at the right. Then identify the quadrant in which each point lies. 30. *A* 32. *C*



CONTENTS

On graph paper, draw a coordinate plane. Then graph and label each point.

34.	E(1, -4)	35 . <i>F</i> (−5, 2)
36.	G(-2, -3)	37 . <i>H</i> (4, 0)

Example 5 Name the ordered pair for point *W* graphed at the right. Then identify the quadrant in which point *W* lies.



The ordered pair is (-4, -5). Point *W* is in quadrant III.

Example 6 Graph and label the point S(3, -1).

Draw a coordinate plane. Move 3 units to the right. Then move 1 unit down. Draw a dot and label it S(3, -1).



Mixed Problem Solving For mixed problem-solving practice, see page 598.

Adding Integers (pp. 120–124)

Add.	
38. -6 + 8	39 4 + (-9)
40. 7 + (-12)	41 18 + 18

42. FOOTBALL On the first play of the game, the Bulldogs lost 8 yards. On the second and third plays, they gained 5 yards and then lost 2 yards. Find the result of the first three plays.



So,
$$-4 + 3 = -1$$
.

3-5	Subtractin
_	6 1 1 1

g integers (pp. 128–131)

Subtract.					
43. -5 - 8	44. 3 – 6				
45. 5 - (-2)	46 . $-4 - (-8)$				

Example 8 Find -3	- 9.
-3 - 9 = -3 + (-9)	To subtract 9, add -9.
= -12	Simplify.

Multiplying Integers (pp. 134–137)

Multiply

widinpiy.	
47 4(3)	48. 8(-6)
49 5(-7)	50 2(40)

ALGEBRA Evaluate each expression if

a = -4, b = -7, and c = 5. **51**. *ab* **52.** -3c**53**. bc **54**. *abc*

Example 9 Find -4(3). -4(3) = -12 The integers have different signs. The product is negative.

Example 10 Evaluate xyz if x = -6, y = 11, and z = -10. xyz = (-6)(11)(-10) x = -6, y = 11, z = -10= (-66)(-10)Multiply -6 and 11. = 660Multiply -66 and -10.

Dividing Integers (pp. 138–141)

Divide.

55 . −45 ÷ (−9)	56 . 36 ÷ (−12)
57 . −12 ÷ 6	58 . −81 ÷ (−9)

59. HIKING Marta started a hike at sea level and ended the hike 6 hours later at 300 feet below sea level. If Marta hiked at the same pace during the trip, how far did she travel each hour?

CONTENTS

Example 11 Find $-72 \div (-9)$. $-72 \div (-9) = 8$ The integers have the same sign. The quotient

is positive.

Practice Test

Vocabulary and Concepts

CHAPTER

- 1. Explain what it means for two numbers to be opposites.
- 2. Name the rule for dividing integers with different signs.

Skills and Applications

Write an integer for each situation. **3**. a stock increased by \$5 **4**. 1000 B.C. 5. an elevator goes down 11 floors Replace each ● with < or > to make a true sentence. 7. 9 • -12 8. |-7| = 9**6**. −3 • −9 9. **WEATHER** The local weather service records the following changes in temperature during the last week: 4, -7, -3, 2, 9, -8, 1. Order these temperature changes from greatest to least. Name the ordered pair for each point graphed at the right. Q Then identify the quadrant in which each point lies. **10**. P 11. *O* **12**. R 0 x Add, subtract, multiply, or divide. **13.** -3 + 814. 12 + (-19)**15**. -3 - 8 **16.** -7 - (-20)**19.** $-24 \div 8$ **18.** 5(-11) **20.** $-36 \div (-9)$ **17.** -7(-3)**ALGEBRA** Evaluate each expression if a = -5, b = 4, and c = -12. **21.** *c* – *a* **22**. *ab* **23**. $ac \div b$

24. **STOCK MARKET** The value of a stock went down \$3 each week for a period of seven weeks. Describe the change in the value of the stock at the end of the seven week period.

Standardized Test Practice

25. MULTIPLE CHOICE Choose the graph that shows the ordered pair (2, -1).





CONTENTS

B



U			4	y			
		_					-
			0				x
	-		0			п	X
			0		-	D	x
	-		 0		-	D	X



Standardized Test Practice

PART 1 Multiple Choice

CHAPTER

Record your answers on the answer sheet provided by your teacher or on a sheet of paper.

- 1. The table shows the Number Language five most common of People languages spoken in 26,745,067 Spanish the United States Chinese 1,976,564 other than English. French 1,914,918 How many more German 1,224,213 people speak Tagalog 1,184,939 Chinese than French? Source: U.S. Census Bureau (Lesson 1-1) **B** 1,914,918 ▲ 61,646 **D** 3,891,482 C 1,976,564 **2.** Which is equivalent to 5^4 ? (Lesson 1-2) **(F)** 20 **G** 125 **⊕** 5 · 5 · 5 · 5 \bigcirc 4 · 4 · 4 · 4 · 4 3. How many millimeters are in 13 centimeters? (Lesson 1-8) **A** 0.13 **B** 1.3 C 13 **D** 130 4. Salvador recorded the number of minutes it took him to drive to work each day for a week. Find the mean for the following times: 12, 23, 10, 14, and 11. (Lesson 2-4) **(F)** 12 min • 13 min **I** 14 min ① 15 min
- 5. Find the interquartile range of the data in the box-and-whisker plot. (Lesson 2-6)



- 6. What is the value of |-2|? (Lesson 3-1) **●** -2 **G** −1 **H** () $\bigcirc 2$
- 7. Which of these is the correct order of the integers from greatest to least? (Lesson 3-2)

▲ 0, 1, -2, -5 ■ 1,0,-2,-5 **○** -5, -2, 0, 1 **○** 1, -2, -5, 0

- 8. Which of these are the coordinates of point Z? (Lesson 3-3) **(2, 2) G** (3, 3) ⊕ (-2, -2) \bigcirc (-3, -3)

		-	y				
						Ζ	
					Υ		
		0					x
		,		Χ			

9. If you graph and connect the following points on a coordinate plane, what shape would you make? (Lesson 3-3)



TEXT-TAKING TIP

CONTENTS

Question 10 Always be sure to check every answer choice of a multiple-choice question. Start with answer choice F. Each time you find an incorrect answer choice, cross it off so you remember that you've eliminated it.

Preparing for Standardized Tests For test-taking strategies and more practice, see pages 608–625.

PART 2 Short Response/Grid In

Record your answers on the answer sheet provided by your teacher or on a sheet of paper.

- Wallpaper costs \$16 per roll, and border costs \$9 per roll. If 12 rolls of wallpaper and 6 rolls of border are needed for one room, find the total cost of the wallpaper and border. (Lesson 1-3)
- Each triangle in the figure below is made from three toothpicks. Extend the pattern. Find the number of toothpicks in the fifth figure. (Lesson 1-7)



13. Write 63.5 million in scientific notation. (Lesson 1-9)

For Questions 14 and 15, use the information below.

The graph shows the number of orders taken each hour one day at a fast food restaurant. (Lesson 2-2)



- **14**. About how many orders were taken at 11:00 A.M.?
- **15**. What time of the day appears to be the least busy at this restaurant?



The temperature of the liquid in Connor's beaker changed drastically. The temperatures he recorded were $-28^{\circ}F$, $59^{\circ}F$, $1^{\circ}F$, $-16^{\circ}F$, $24^{\circ}F$, and $8^{\circ}F$. (Lesson 3-2)

- **16**. Order the temperatures from least to greatest.
- **17**. Find the mean temperature.
- **18**. When Elena went hiking at 8 A.M., she started at an elevation of 16 meters below sea level. But at 2 P.M., she was 12 meters higher than when she started. What was Elena's elevation at 2 P.M.? (Lesson 3-5)

19. Find
$$\frac{-12 + 8(-3)}{-2 - 7}$$
. (Lesson 3-7)

PART 3 Extended Response

Record your answers on a sheet of paper. Show your work.

20. Use the table of ordered pairs at the right to answer the questions below. (Lesson 3-3)

x	y
-2	1
3	2
-1	-4

- a. Plot the ordered pairs in the table on a coordinate plane.
- **b.** In which quadrant is a point on the graph not represented?
- **c.** Connect the points on the graph. What shape do they form?
- **d.** How would you double the size of the figure you drew above?
- e. Add four more columns to the table. Label the columns x + y, x - y, xy, and $x \div y$. Complete the table.

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